

# Muon EDM, g-2, and Flavor Violation From Physics Beyond the Standard Model

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# Outline

## Beyond the SM Scenarios:

- *Supersymmetry*
- *Neutrino Masses*
- *Grand Unification*
- *Flavor Symmetry*
- *Other (TeV scale extra matter, ..)*

## Effects on Muon Properties:

- *(g-2)*
- *Electric Dipole Moment (EDM)*
- *Lepton Flavor Violation*

$\mu \rightarrow e\gamma$

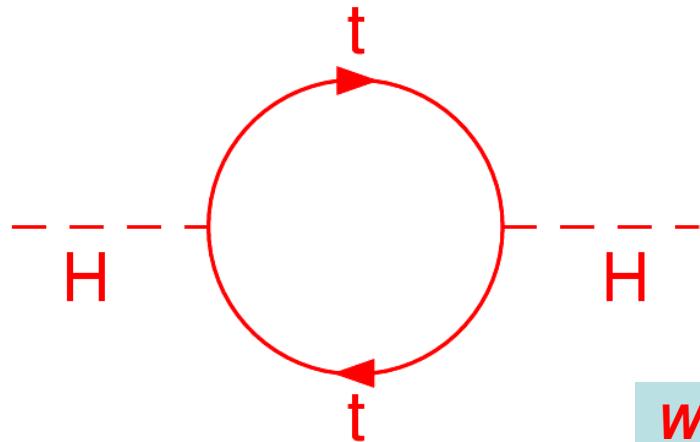
$\mu - e$  conversion

## Related Processes:

- *EDM of electron, neutron, deuteron*
- $\tau \rightarrow \mu\gamma$

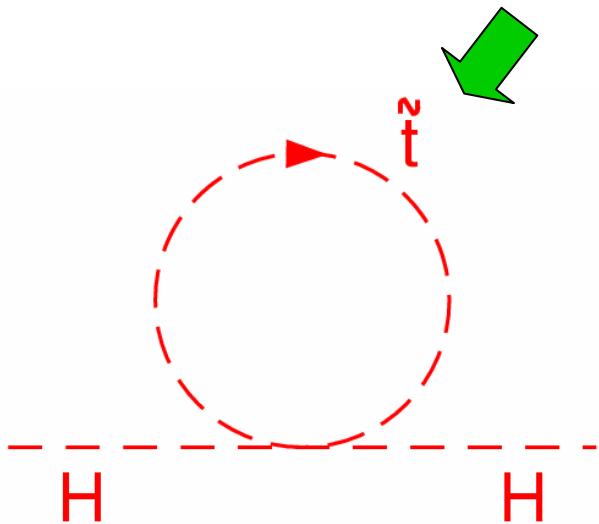
## Conclusions

# Stability of Higgs Mass



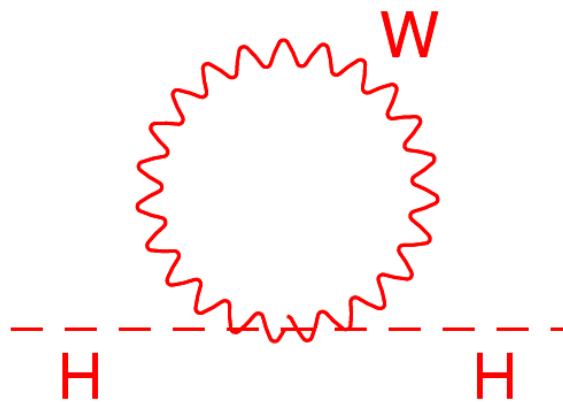
$$\Delta m_H^2 = -\frac{\lambda_t^2}{8\pi^2} \Lambda^2$$

*With SUSY, Quadratic Divergence Cancels*

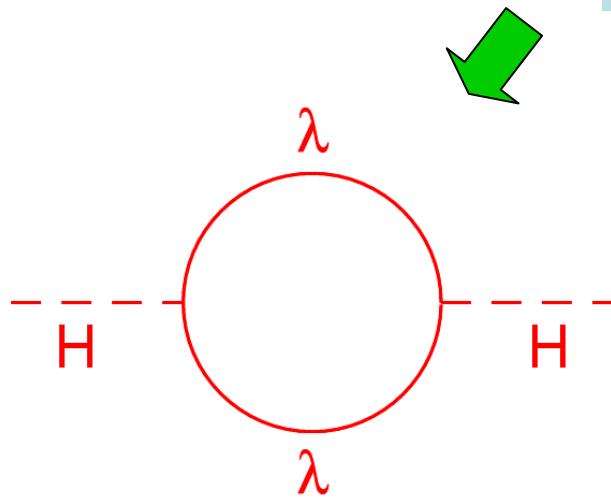


$$\Delta m_H^2 = +\frac{\lambda_t^2}{8\pi^2} \Lambda^2$$

$$m_{\tilde{t}}^2 - m_t^2 \lesssim (\text{TeV})^2$$



*With SUSY, gauge boson contribution is cancelled by gaugino contribution.*

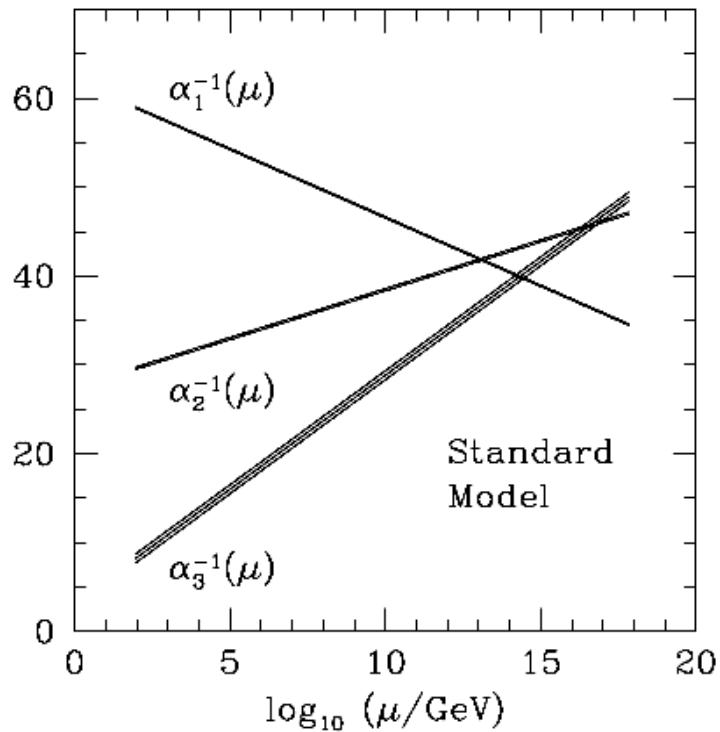


# SUSY Spectrum

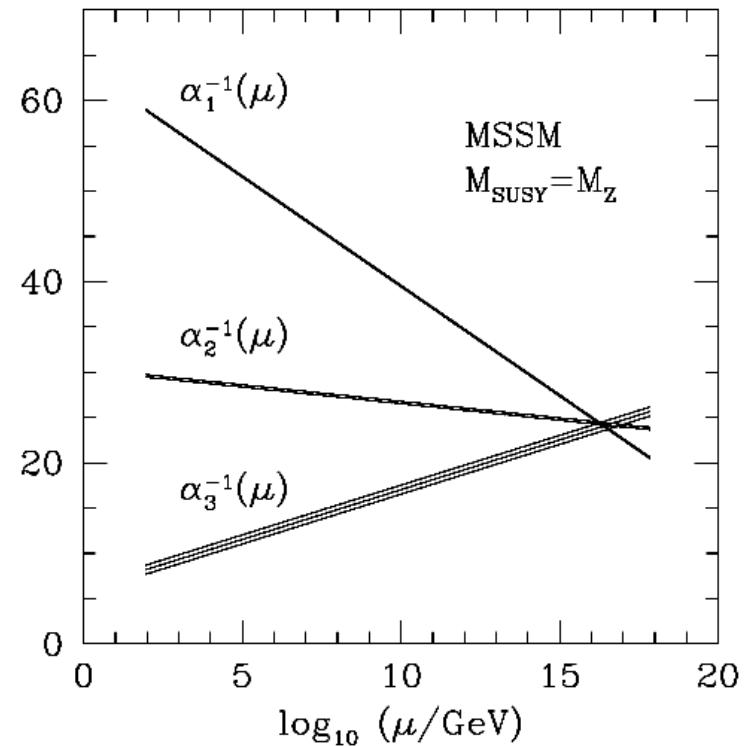
SM Particles		SUSY Partners	
Spin = 1/2	$Q$	$\tilde{Q}$	
	$u^c$	$\tilde{u}^c$	
	$d^c$	$\tilde{d}^c$	Spin = 0
	$L$	$\tilde{L}$	
Spin = 0	$e^c$	$\tilde{e}^c$	
	$H_u$	$\tilde{H}_u$	
	$H_d$	$\tilde{H}_d$	Spin = 1/2
	$g$	$\tilde{g}$	
Spin = 1	$W$	$\tilde{W}$	Spin = 1/2
	$B$	$\tilde{B}$	

$$R = (-1)^{3B+L+2S}$$

# Evolution of Gauge Couplings



Standard Model



Supersymmetry

## Structure of Matter Multiplets

$$Q = \begin{pmatrix} u_1 & u_2 & u_3 \\ d_1 & d_2 & d_3 \end{pmatrix} \sim (3, 2, \frac{1}{6})$$

$$u^c = (u_1^c \quad u_2^c \quad u_3^c) \sim (\bar{3}, 1, \frac{-2}{3})$$

$$d^c = (d_1^c \quad d_2^c \quad d_3^c) \sim (\bar{3}, 1, \frac{1}{3})$$

$$L = \begin{pmatrix} \nu \\ e^- \end{pmatrix} \sim (1, 2, \frac{-1}{2})$$

$$e^c \sim (1, 1, +1)$$

$$\nu^c \sim (1, 1, 0)$$

## Matter Unification in 16 of SO(10)



$u_1$	:	$  \uparrow\downarrow\uparrow\uparrow\downarrow >$
$u_2$	:	$  \uparrow\downarrow\uparrow\downarrow\uparrow >$
$u_3$	:	$  \uparrow\downarrow\downarrow\uparrow\uparrow >$
$d_1$	:	$  \downarrow\uparrow\uparrow\uparrow\downarrow >$
$d_2$	:	$  \downarrow\uparrow\uparrow\downarrow\uparrow >$
$d_3$	:	$  \downarrow\uparrow\downarrow\uparrow\uparrow >$
$u_1^c$	:	$  \downarrow\downarrow\uparrow\downarrow\downarrow >$
$u_2^c$	:	$  \downarrow\downarrow\downarrow\uparrow\downarrow >$
$u_3^c$	:	$  \downarrow\downarrow\downarrow\downarrow\uparrow >$
$d_1^c$	:	$  \uparrow\uparrow\uparrow\downarrow\downarrow >$
$d_2^c$	:	$  \uparrow\uparrow\downarrow\uparrow\downarrow >$
$d_3^c$	:	$  \uparrow\uparrow\downarrow\downarrow\uparrow >$
$\nu$	:	$  \uparrow\downarrow\downarrow\downarrow\downarrow >$
$e$	:	$  \downarrow\uparrow\downarrow\downarrow\downarrow >$
$e^c$	:	$  \downarrow\downarrow\uparrow\uparrow\uparrow >$
$\nu^c$	:	$  \uparrow\uparrow\uparrow\uparrow\uparrow >$

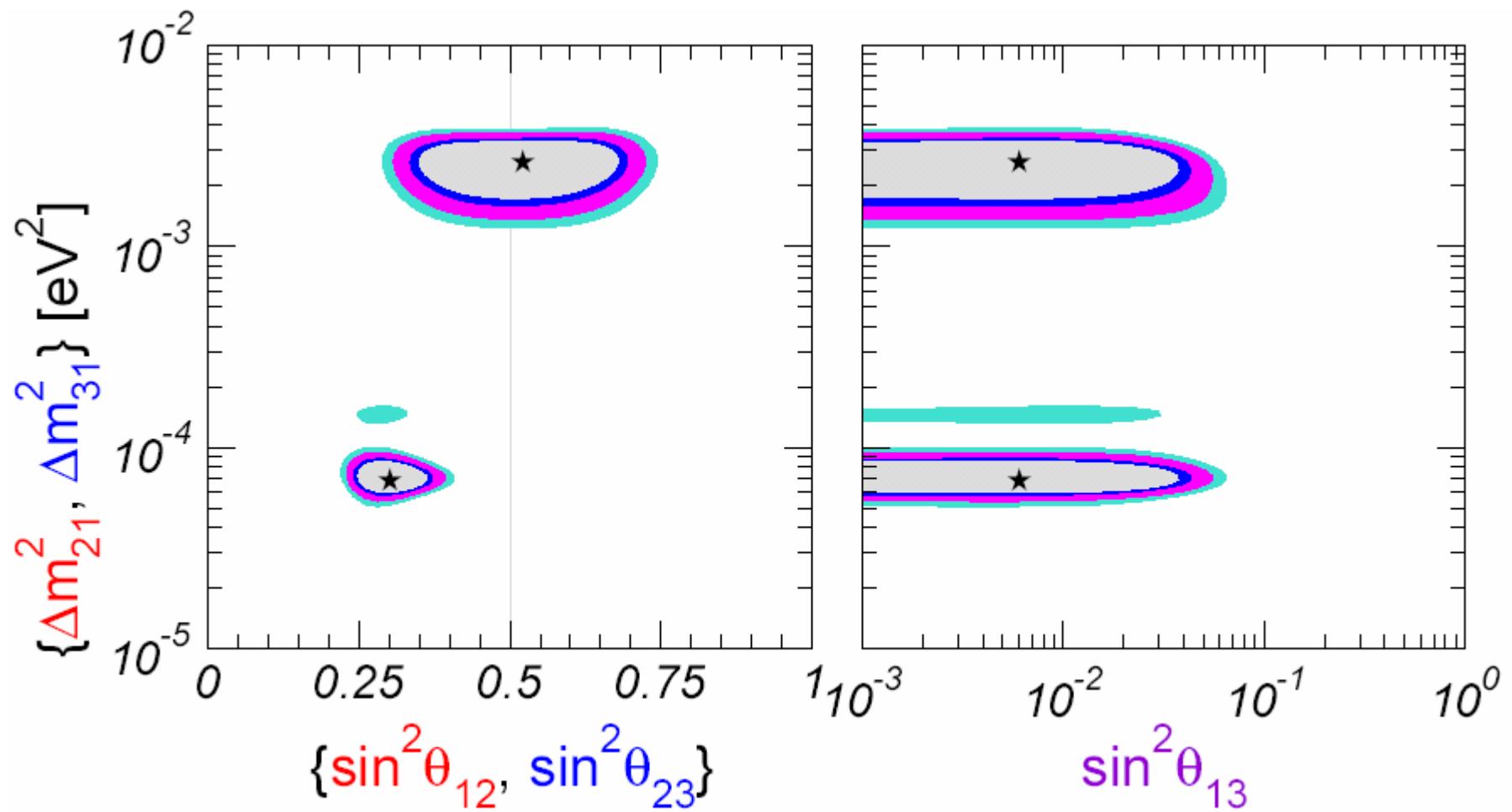
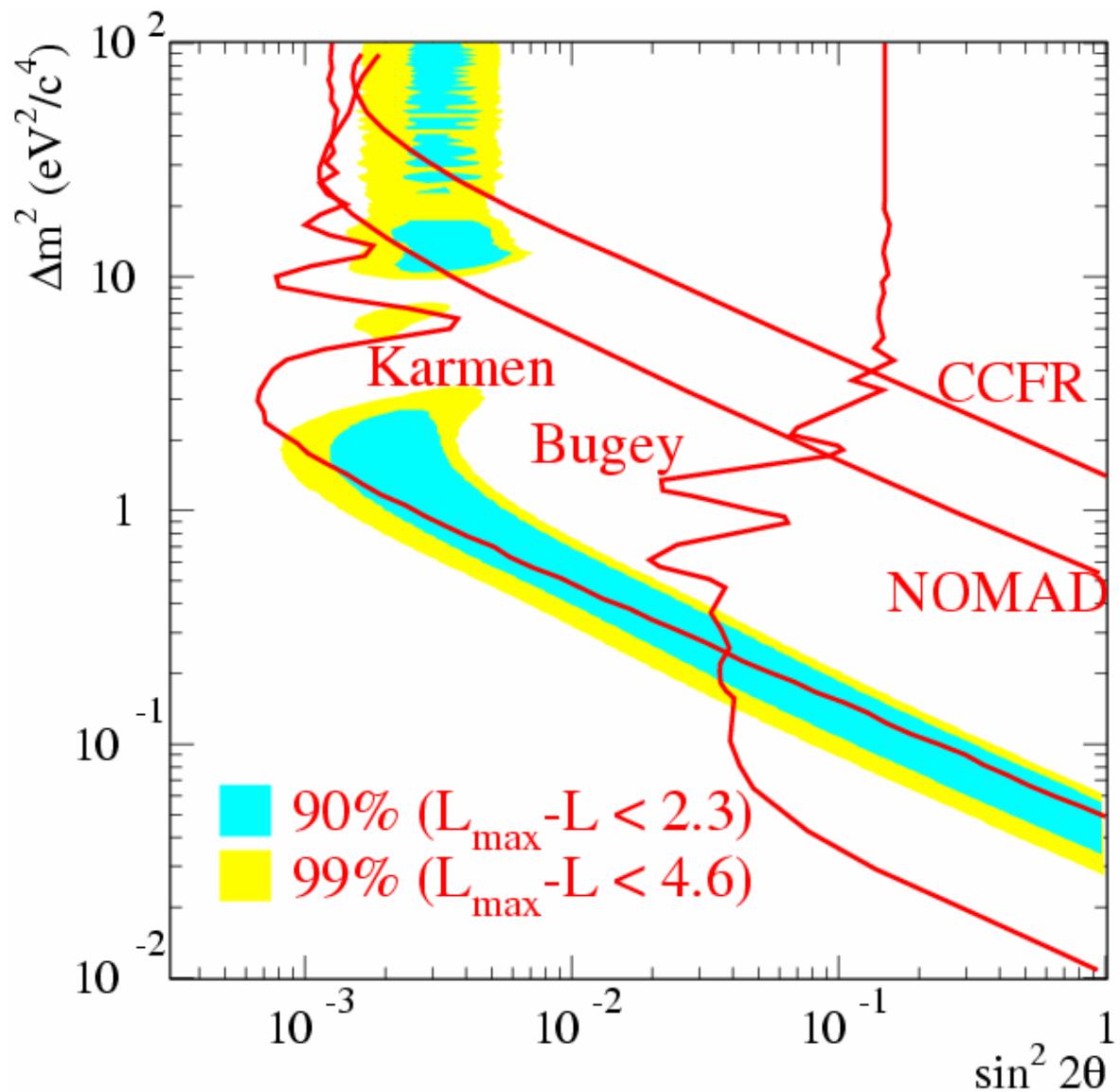
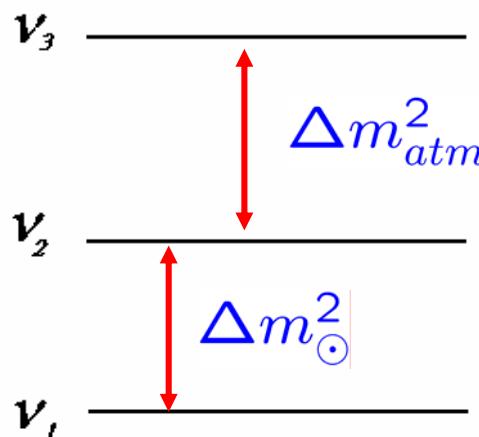


Figure 10: Projections of the allowed regions from the global oscillation data at 90%, 95%, 99%, and 3 $\sigma$  C.L. for 2 d.o.f. for various parameter combinations.

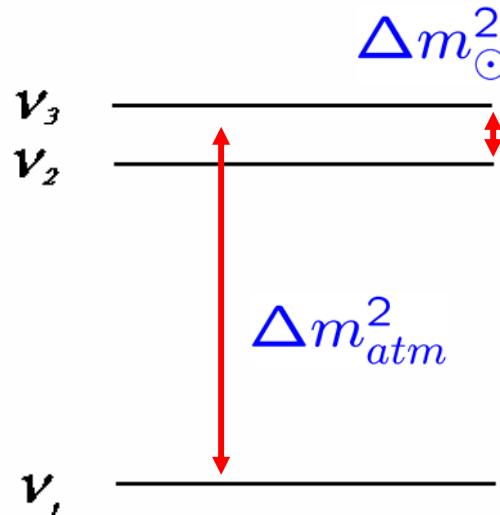
# LSND



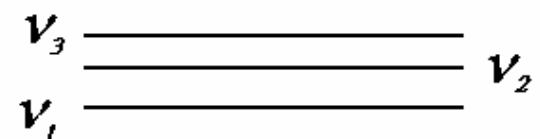
# Patterns of Neutrino Mass Spectrum



Normal Hierarchy



Inverted Hierarchy



Quasi-degenerate

# Neutrino Mixing versus Quark Mixing

Leptons

$$U_\ell = \begin{pmatrix} 0.85 & -0.52 & 0.053 \\ 0.33 & 0.62 & -0.72 \\ -0.40 & -0.59 & -0.70 \end{pmatrix}$$

Quarks

$$V_q = \begin{pmatrix} 0.976 & 0.22 & 0.003 \\ -0.22 & 0.98 & 0.04 \\ 0.007 & -0.04 & 1 \end{pmatrix}$$

Disparity a challenge for Quark-Lepton unified theories.

# Neutrino Masses and the Scale of New Physics

$$\mathcal{L} = \frac{LLHH}{M_R}$$

$\langle H \rangle \sim 246$  GeV and  $m_{\nu_3} \sim 0.05$  eV

*from atmospheric neutrino oscillation data*



$m_R \sim 10^{14} - 10^{15}$  GeV

**Very close to the GUT scale.**

Leptogenesis via  $\nu_R$  decay explains cosmological baryon asymmetry

## Muon ( $g - 2$ ) in Supersymmetric Models

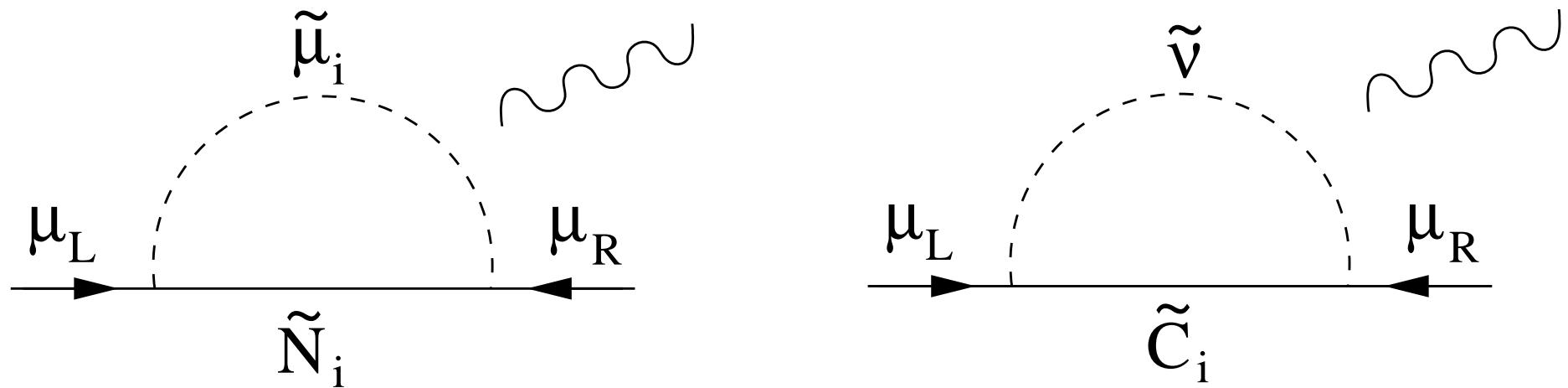


Figure 1: Neutralino and Chargino diagrams for muon ( $g - 2$ ).

$$L = \frac{ie}{2m_\mu} F(q^2) \bar{u}(p_f) \sigma_{\mu\nu} q^\mu \epsilon^\nu u(p_i)$$

$$\begin{aligned}
g_\mu^{(C)} = & \frac{1}{48\pi^2} \frac{m_\mu^2}{m_{\tilde{\nu}_X}^2} |C_{2AX}^{L(l)}|^2 \frac{2 + 3x_{AX} - 6x_{AX}^2 + x_{AX}^3 + 6x_{AX} \ln x_{AX}}{(1 - x_{AX})^4} \\
& + \frac{1}{16\pi^2} \frac{m_\mu M_{\tilde{\chi}_A^-}}{m_{\tilde{\nu}_X}^2} C_{2AX}^{L(l)} C_{2AX}^{R(l)*} \frac{-3 + 4x_{AX} - x_{AX}^2 - 2 \ln x_{AX}}{(1 - x_{AX})^3} \\
& +(L \leftrightarrow R)
\end{aligned}$$

$$\begin{aligned}
g_\mu^{(N)} = & -\frac{1}{48\pi^2} \frac{m_\mu^2}{m_{\tilde{l}_X}^2} |N_{2AX}^{L(l)}|^2 \frac{1 - 6x_{AX} + 3x_{AX}^2 + 2x_{AX}^3 - 6x_{AX}^2 \ln x_{AX}}{(1 - x_{AX})^4} \\
& - \frac{1}{16\pi^2} \frac{m_\mu M_{\tilde{\chi}_A^0}}{m_{\tilde{l}_X}^2} N_{2AX}^{L(l)} N_{2AX}^{R(l)*} \frac{1 - x_{AX}^2 + 2x_{AX} \ln x_{AX}}{(1 - x_{AX})^3} \\
& +(L \leftrightarrow R),
\end{aligned}$$

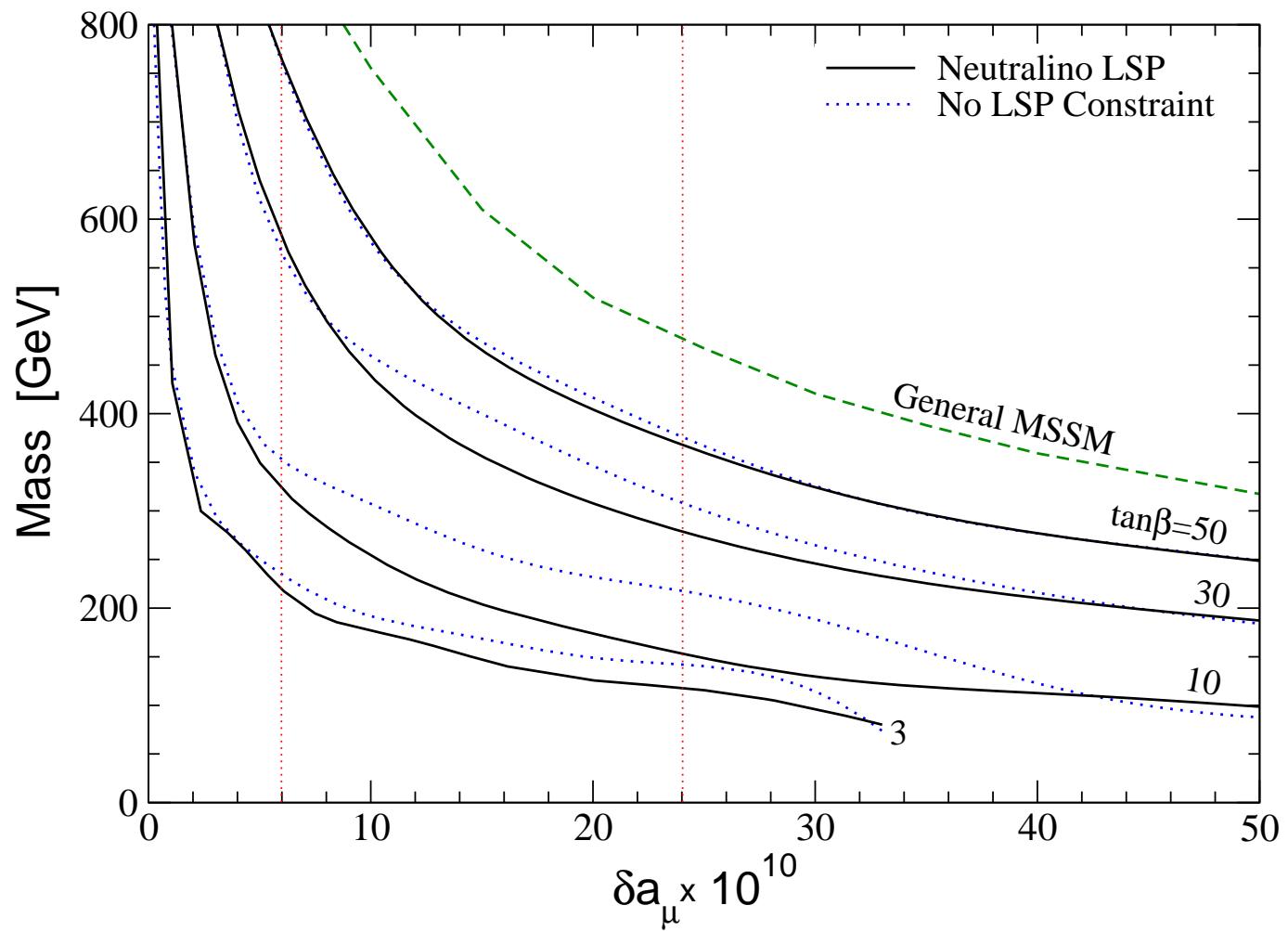


Figure 2: LSP mass vs.  $\delta a_\mu$ .

M. Byrne, C. Kolda and J.E. Lennon, hep-ph/0208067.

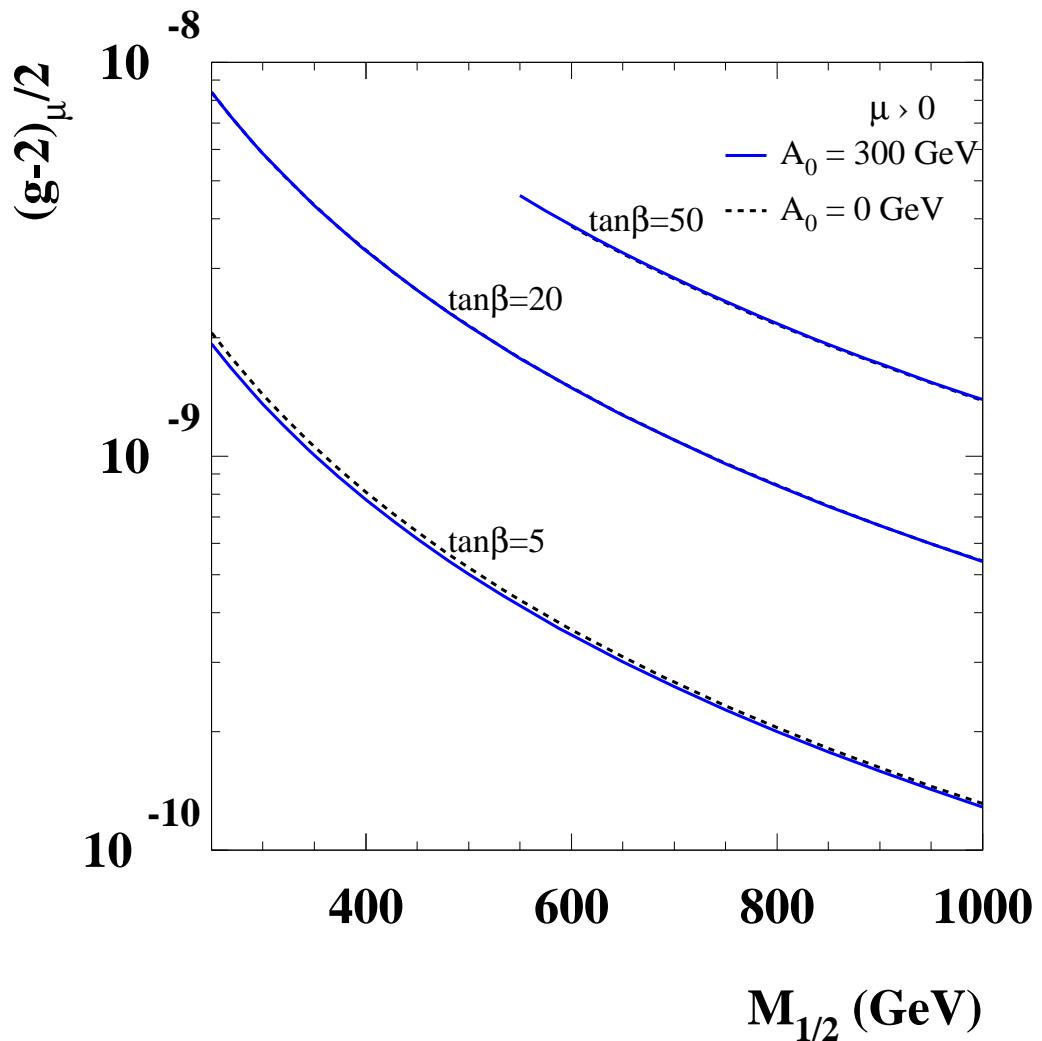


Figure 3: Muon Anomalous Magnetic Moment.

Ts. Enkhbat, KSB

# Lepton Flavor Violation and Neutrino Mass

Seesaw mechanism naturally explains small ν-mass.

$$\mathcal{L} = \bar{\nu}_L M_D \nu_R + \frac{1}{2} \nu_R^T M_R \nu_R + h.c.$$

$$M_\nu = -M_D M_R^{-1} M_D^T$$

Current neutrino-oscillation data suggests

$$M_R \sim (10^{12} - 10^{15}) \text{ GeV}$$

Flavor change in neutrino-sector



Flavor change in charged leptons

In standard model with seesaw, leptonic flavor changing is very tiny.

$$Br(\mu \rightarrow e\gamma) \propto \frac{1}{M_R^4} \sim 10^{-50}$$

# In Supersymmetric Standard Model

$$Br(\mu \rightarrow e\gamma) \propto \frac{1}{M_{SUSY}^4} \sim 10^{-10}$$

For  $M_R \leq \mu \leq M_{Pl}$   $\nu_R$  active

→ flavor violation in neutrino sector transmitted to Sleptons

Borzumati, Masiero (1986)

Hall, Kostelecky, Raby (1986)

Hisano et. al., (1995)

Hisano, Okada (1998)

## SUSY Seesaw Mechanism

$$\mathcal{W} = f \nu^c \nu^c \Delta + Y_\nu \nu^c L H_u$$

$$M_D = Y_\nu v_u ; M_R = f v_{B-L}$$

If  $B-L$  is gauged,  $M_R$  must arise through Yukawa couplings.

Flavor violation may reside entirely in  $f$  or entirely in  $Y_\nu$

**If flavor violation occurs only in Dirac Yukawa  $Y_\nu$  (with mSUGRA)**

$$\Delta m_{ij}^2 (i \neq j) \simeq -\frac{1}{8\pi^2} (3m_0^2 + A_0^2) (Y_\nu^\dagger Y_\nu)_{ij} \left( \ln \frac{M_{Pl}}{M_{B-L}} \right)$$

**If flavor violation occurs only in  $f$  (Majorana LFV)**

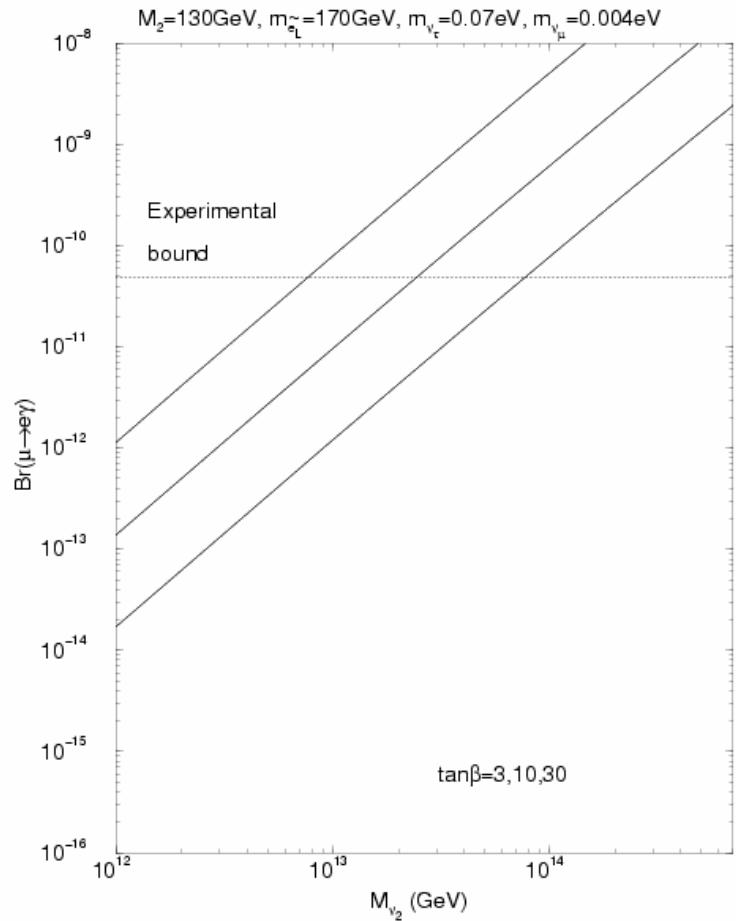
$$A_{\ell ij} (i \neq j) \simeq \frac{-3}{64\pi^4} [A_\ell (Y_\nu^\dagger Y_\nu f^\dagger f + f^\dagger f Y_\nu^\dagger Y_\nu)]_{ij} \left( \ln \frac{M_{Pl}}{M_{B-L}} \right)^2$$

$$\Delta m_{ij}^2 (i \neq j) \simeq \frac{-3(m_0^2 + A_0^2)}{32\pi^4} [Y_\nu^\dagger Y_\nu f^\dagger f + f^\dagger f Y_\nu^\dagger Y_\nu]_{ij} \left( \ln \frac{M_{Pl}}{M_{B-L}} \right)^2$$

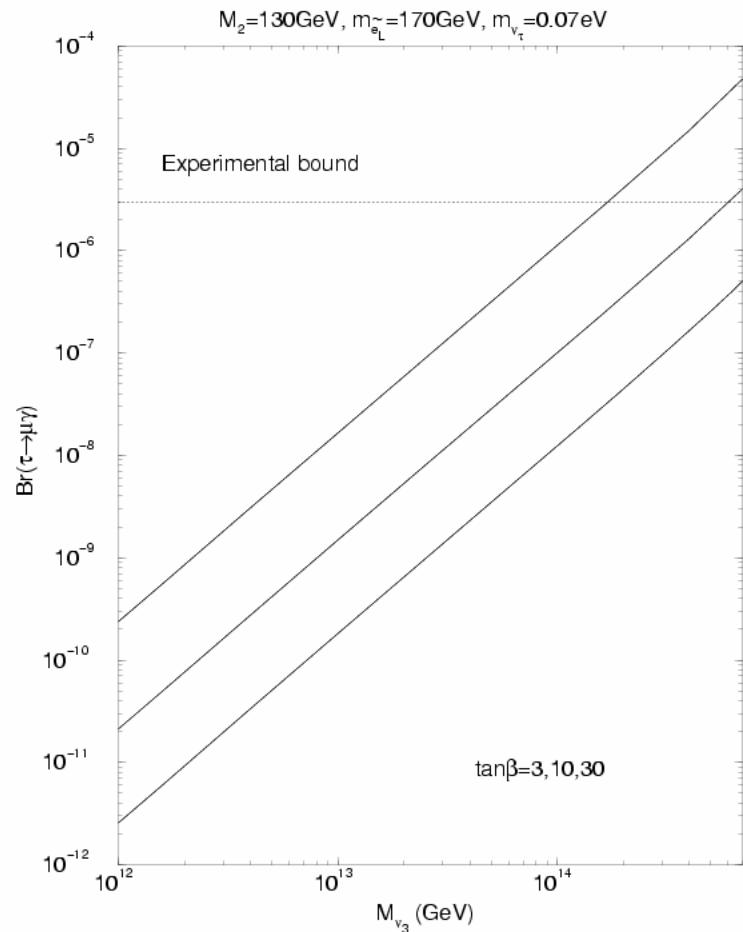
**LFV in the two scenarios are comparable.**

**More detailed study is needed.**

### $\mu \rightarrow e\gamma$ in the MSSMRN with the MSW large angle solution



### $\tau \rightarrow \mu\gamma$ in the MSSMRN



**LFV from Dirac neutrino Yukawa couplings**

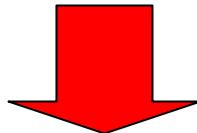
**Hisano, Okada, (1998)**

# LFV from Majorana Yukawa Couplings

Minimal SUSY Left-Right Symmetric Model    Dutta, Mohapatra, KSB (2002)

$$v_{B-L} = 2 \times 10^{12} \text{ GeV}, M_D \propto M_{l+}$$

$$f = \begin{pmatrix} -1.1 \times 10^{-4} & -0.015 & 0.29 \\ -0.015 & 0.50 & -0.57 \\ 0.29 & -0.57 & 0.104 \end{pmatrix}$$



$$(m_1, m_2, m_3) = (-2.7 \times 10^{-3}, 6.4 \times 10^{-3}, 8.6 \times 10^{-2}) \text{ eV}$$

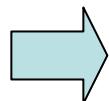
$$U = \begin{pmatrix} 0.85 & -0.52 & -0.053 \\ 0.33 & 0.62 & -0.72 \\ -0.40 & -0.59 & -0.70 \end{pmatrix}$$

Relevant for Leptogenesis: Baryon asymmetry can be related to neutrino oscillation parameters

**For Dirac LFV scenario**

$$M_R = (9 \times 10^{13} \text{ GeV}) \times (\text{Identity Matrix})$$

$$Y_\nu = \begin{pmatrix} 0.04 + 0.074i & -0.073 + 0.029i & 0.025 - 0.034i \\ -0.073 + 0.029i & -0.22 + 0.011i & -0.35 - 0.013i \\ 0.025 - 0.034i & -0.35 - 0.013i & -0.24 + 0.016i \end{pmatrix}$$



**Same neutrino oscillation parameters as in Majorona LFV**

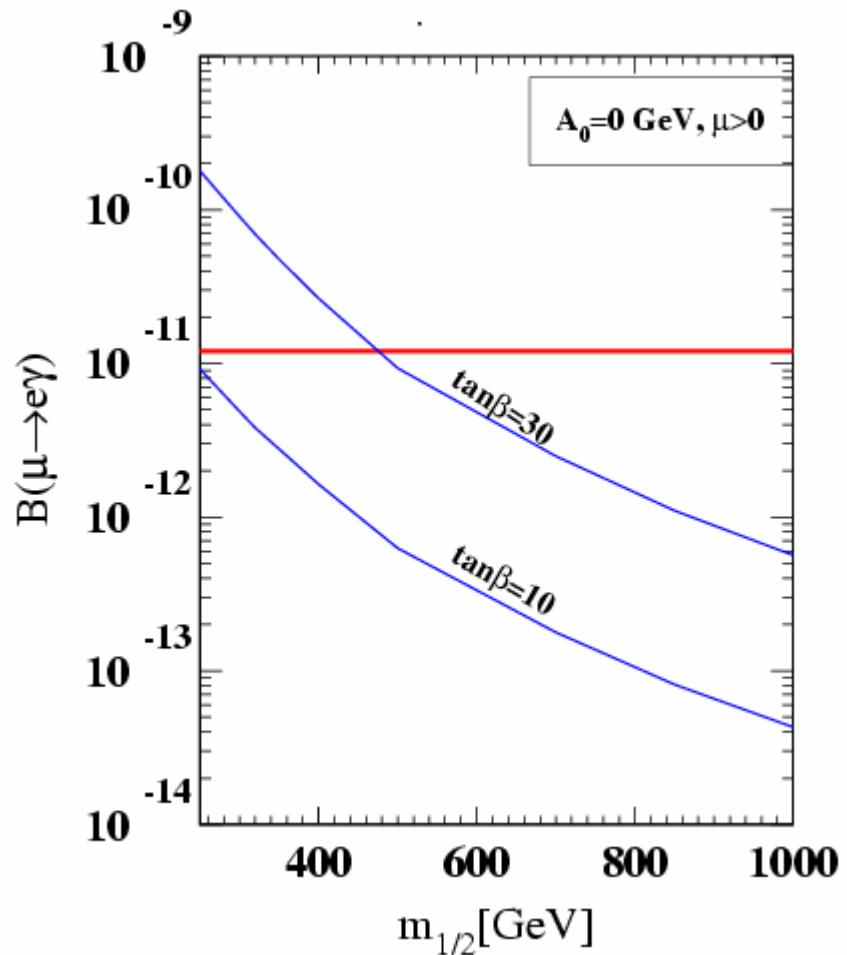
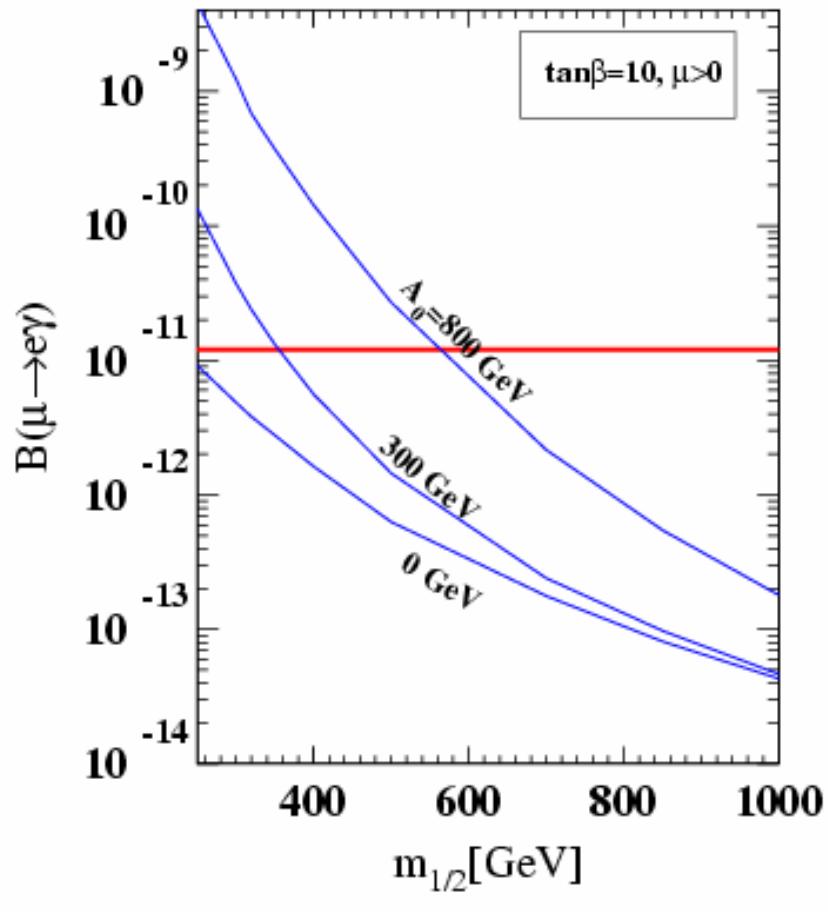
**The two scenarios differ in predictions for**

$$\mu \rightarrow e\gamma$$

$$\tau \rightarrow \mu\gamma$$

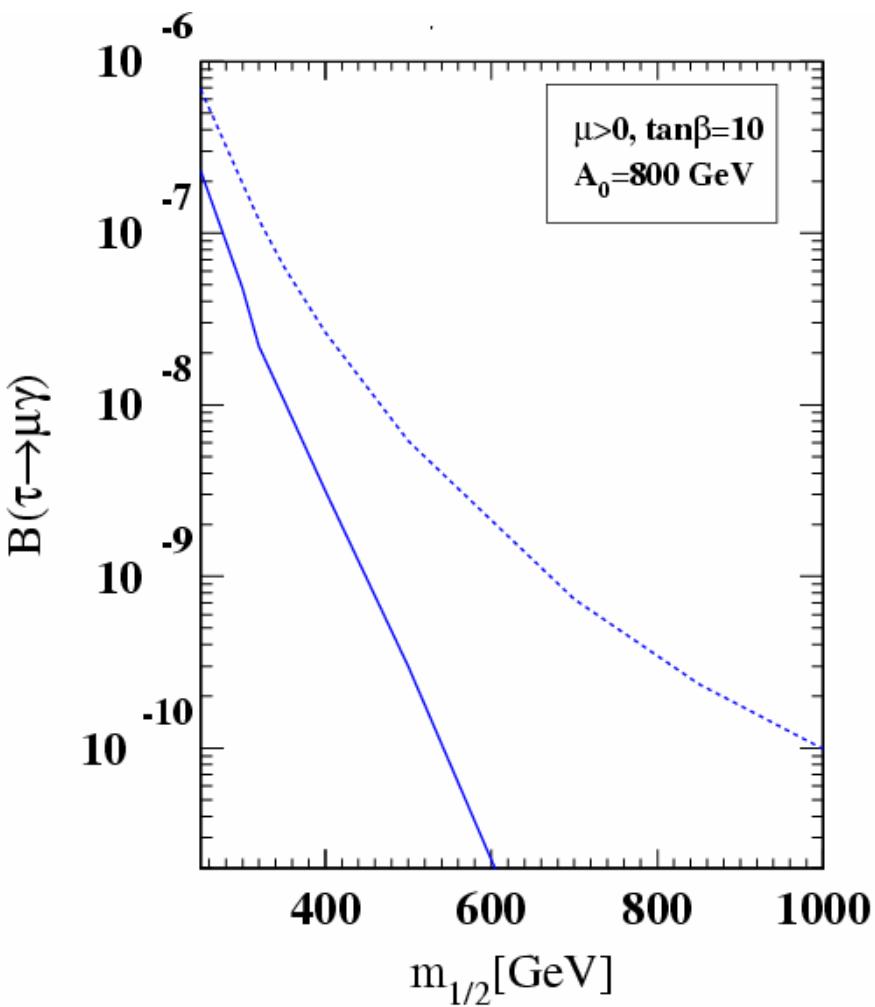
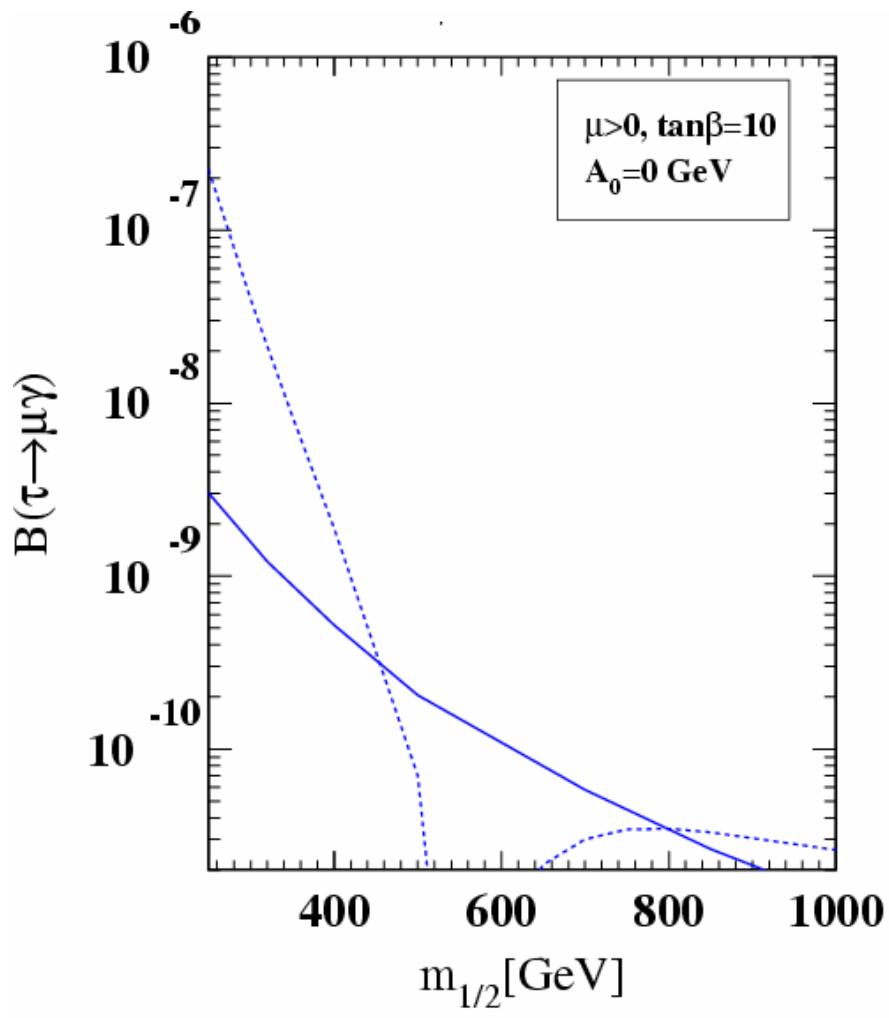
$$\tau \rightarrow e\gamma$$

$\mu \rightarrow e\gamma$  Majorana LFV

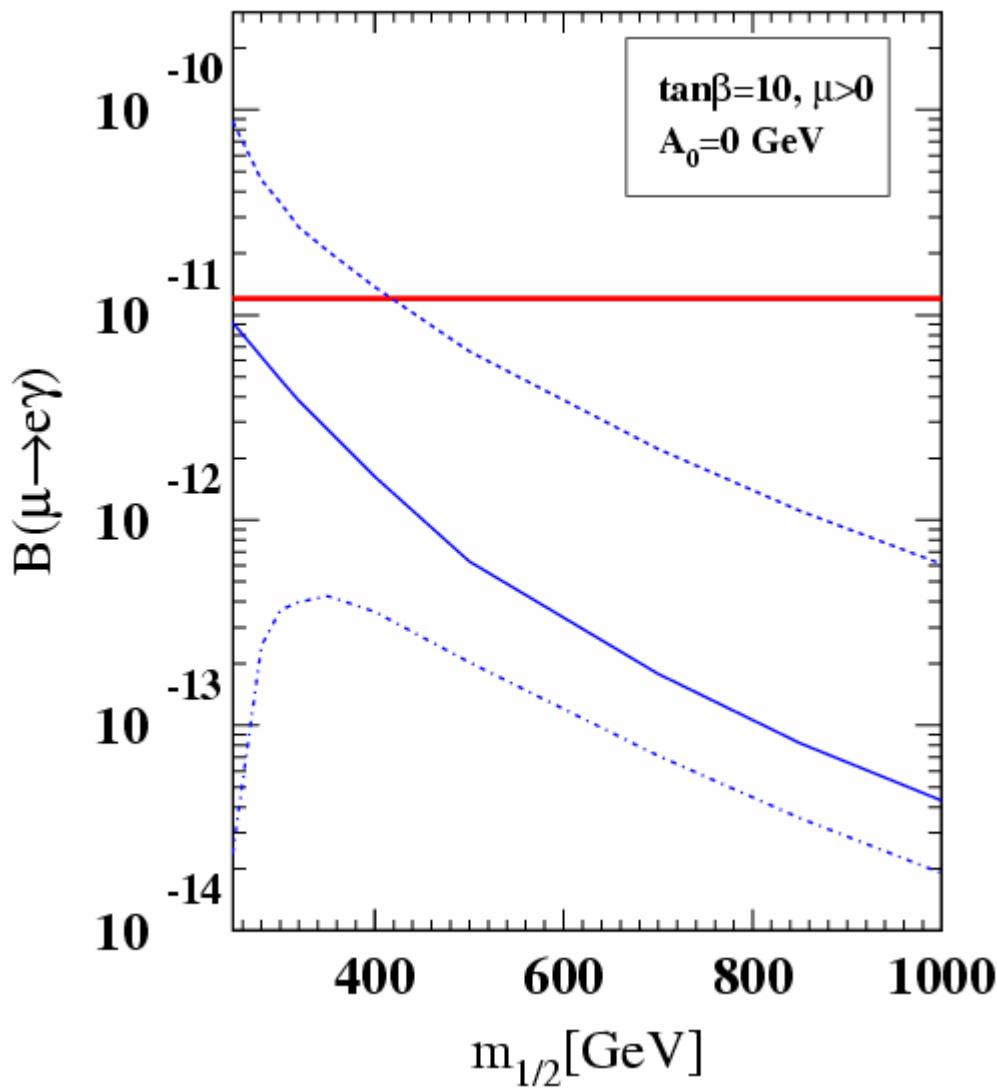


Dutta, Mohapatra, KSB (2002)

$\tau \rightarrow \mu\gamma$  Majorana LFV



# Dirac versus Majorana LFV



Solid line: Majorana LFV  
Dotted line: Dirac LFV

## Flavor Symmetry and Fermion Mass Hierarchy

- Complex Yukawa couplings. SUSY in mSUGRA with real universal soft parameters.
- Fermion mass matrices:

$$M_u \sim \langle H_u \rangle \begin{pmatrix} \epsilon^8 & \epsilon^6 & \epsilon^4 \\ \epsilon^6 & \epsilon^4 & \epsilon^2 \\ \epsilon^4 & \epsilon^2 & 1 \end{pmatrix}$$

$$M_d \sim \langle H_d \rangle \epsilon^p \begin{pmatrix} \epsilon^5 & \epsilon^4 & \epsilon^4 \\ \epsilon^3 & \epsilon^2 & \epsilon^2 \\ \epsilon & 1 & 1 \end{pmatrix},$$

$$M_e \sim \langle H_d \rangle \epsilon^p \begin{pmatrix} \epsilon^5 & \epsilon^3 & \epsilon \\ \epsilon^4 & \epsilon^2 & 1 \\ \epsilon^4 & \epsilon^2 & 1 \end{pmatrix}$$

$$M_{\nu_D} \sim \langle H_u \rangle \epsilon^s \begin{pmatrix} \epsilon^2 & \epsilon & \epsilon \\ \epsilon & 1 & 1 \\ \epsilon & 1 & 1 \end{pmatrix},$$

$$M_{\nu^c} \sim M_R \begin{pmatrix} \epsilon^2 & \epsilon & \epsilon \\ \epsilon & 1 & 1 \\ \epsilon & 1 & 1 \end{pmatrix} \quad \text{See-Saw} \Rightarrow \quad M_\nu^{light} \sim \frac{\langle H_u \rangle^2}{M_R} \epsilon^{2s} \begin{pmatrix} \epsilon^2 & \epsilon & \epsilon \\ \epsilon & 1 & 1 \\ \epsilon & 1 & 1 \end{pmatrix}.$$

Here small parameter  $\epsilon \simeq .2$  and  $p = (0, 1, 2)$  for  $\tan \beta = (50, 20, 5)$

- This experimental fact motivates a generation dependent  $U(1)$  symmetry.

### U(1) flavor charge assignment

Field	$U(1)_A$ Charge	Charge notation
$Q_1, Q_2, Q_3$	4, 2, 0	$q_i^Q$
$L_1, L_2, L_3$	$1 + \textcolor{blue}{s}, \textcolor{blue}{s}, \textcolor{blue}{s}$	$q_i^L$
$u_1^c, u_2^c, u_3^c$	4, 2, 0	$q_i^u$
$d_1^c, d_2^c, d_3^c$	$1 + \textcolor{blue}{p}, \textcolor{blue}{p}, \textcolor{blue}{p}$	$q_i^d$
$e_1^c, e_2^c, e_3^c$	$4 + \textcolor{blue}{p} - \textcolor{blue}{s}, 2 + \textcolor{blue}{p} - \textcolor{blue}{s}, \textcolor{blue}{p} - \textcolor{blue}{s}$	$q_i^e$
$\nu_1^c, \nu_2^c, \nu_3^c$	1, 0, 0	$q_i^\nu$
$H_u, H_d, S$	0, 0, -1	$(h, \bar{h}, q_s)$

The value of Yukawa couplings at  $M_F$  from low energy data through two-loop RGE  
( $\tan \beta = 5$ )

$$Y^u = \begin{pmatrix} (1.45 + 1.60 i) \epsilon^8 & (-0.563 - 1.24 i) \epsilon^6 & (1.50 - 0.397 i) \epsilon^4 \\ (-0.769 - 0.584 i) \epsilon^6 & (0.765 - 0.109 i) \epsilon^4 & (-0.255 - 0.261 i) \epsilon^2 \\ (-0.282 - 0.204 i) \epsilon^4 & (0.274 - 0.44 \times 10^{-1} i) \epsilon^2 & 0.554 - 2.80 \times 10^{-5} i \end{pmatrix}$$

$$Y^d = \epsilon^2 \begin{pmatrix} (1.87 - 1.69 i) \epsilon^5 & (1.93 + 0.849 i) \epsilon^4 & (1.29 + 0.957 i) \epsilon^4 \\ (-0.404 - 0.248 i) \epsilon^3 & (0.5542 + 1.54 \times 10^{-2} i) \epsilon^2 & (0.702 - 0.546 i) \epsilon^2 \\ (-0.152 - 0.435 i) \epsilon & 0.312 - 0.314 i & 0.543 - 4.74 \times 10^{-4} i \end{pmatrix}$$

$$Y^e = \epsilon^2 \begin{pmatrix} (3.52 \times 10^{-2} + 0.480 i) \epsilon^5 & (-1.85 - 1.74 i) \epsilon^3 & (-0.539 - 0.579 i) \epsilon \\ (-0.170 - 0.612 i) \epsilon^4 & (1.15 + 4.65 \times 10^{-2} i) \epsilon^2 & 0.319 - 0.321 i \\ (0.538 - 0.421 i) \epsilon^4 & (-0.419 - 0.536 i) \epsilon^2 & 0.784 + 9.74 \times 10^{-5} i \end{pmatrix}$$

$$Y^\nu = \epsilon^2 \begin{pmatrix} (0.232 - 0.190 i) \epsilon^2 & (0.217 - 6.09 \times 10^{-2} i) \epsilon & (-0.206 - 0.637 i) \epsilon \\ (0.638 - 0.652 i) \epsilon & -7.82 \times 10^{-2} + 0.537 i & 0.804 + 0.296 i \\ (0.305 - 0.392 i) \epsilon & -4.41 \times 10^{-3} + 0.277 i & 0.404 - 3.89 \times 10^{-2} i \end{pmatrix}$$

# Anomalous U(1) Symmetry and Lepton Flavor Violation

Enkhbat, Gogoladze, KSB (2003)

$f_a, S, X_k$

$\circlearrowleft$

$\circlearrowright$

$\circlearrowleft$

$\circlearrowright$

$$\delta \left( \tilde{m}_L^2 \right)_{ij}^A \simeq -q_i^L |q_s| g_F^2 \delta_{ij} m_0^2 \text{Tr}(Q) \frac{\ln (M_{st}/M_F)}{8\pi^2}$$

$\lambda_F$

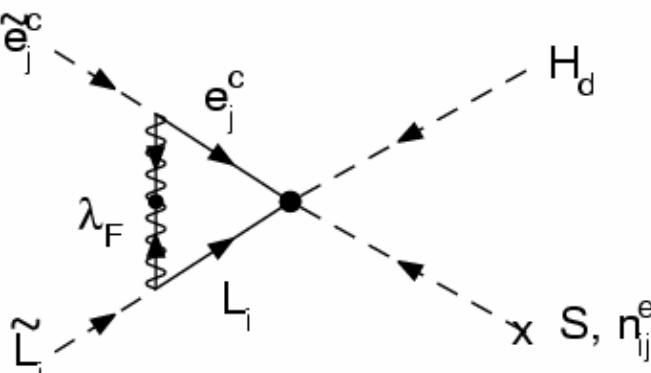
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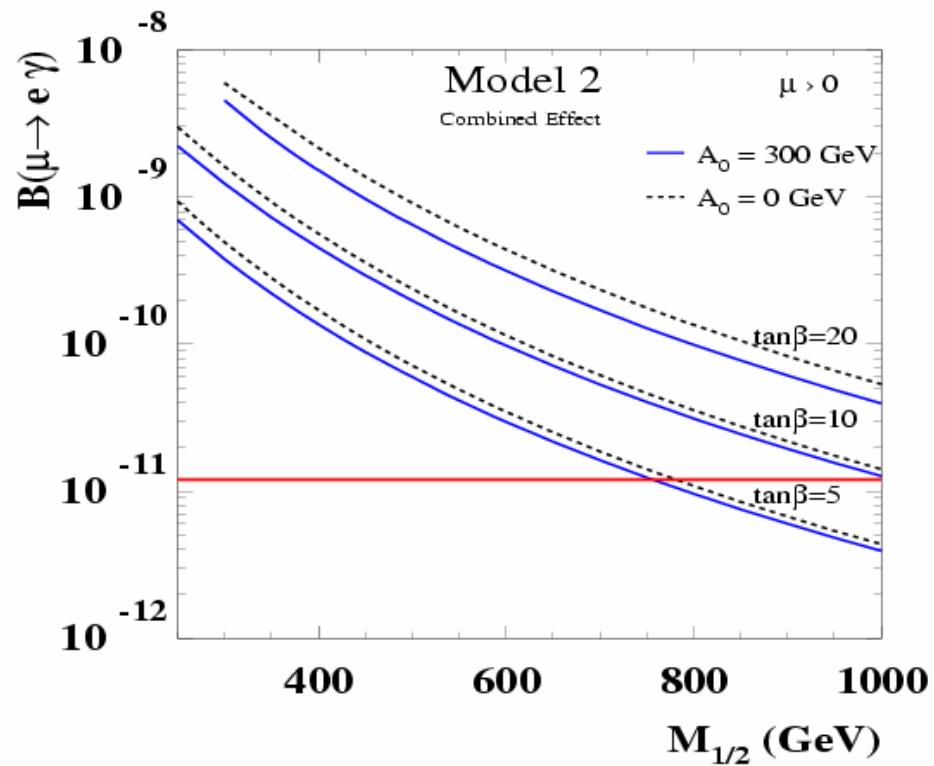
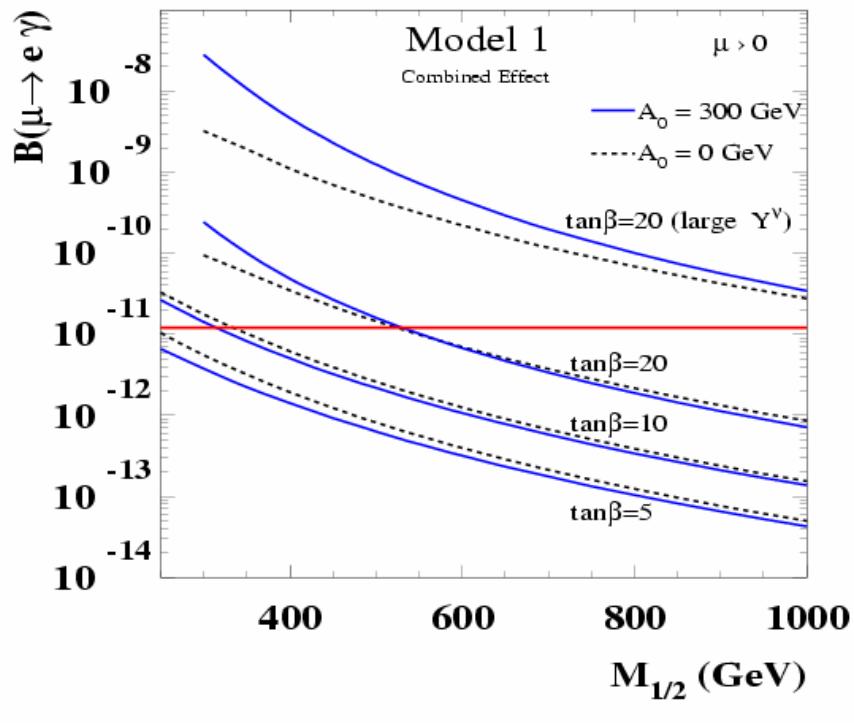
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$$\delta \left( \tilde{m}_L^2 \right)_{ij}^G \simeq (q_i^L g_F)^2 \delta_{ij} (M_{\lambda_F})^2 \frac{\ln (M_{st}/M_F)}{2\pi^2}$$



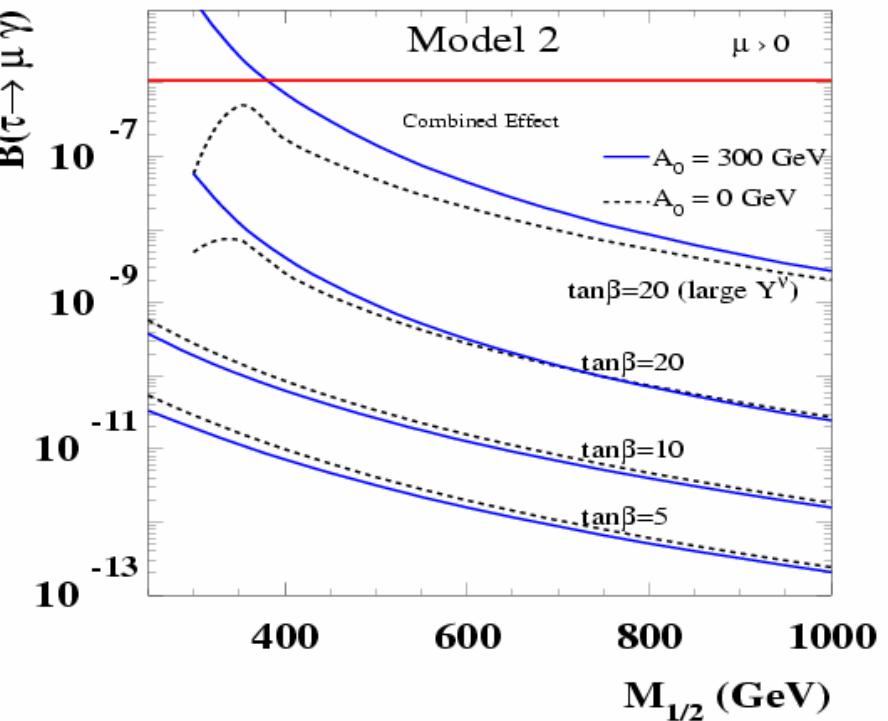
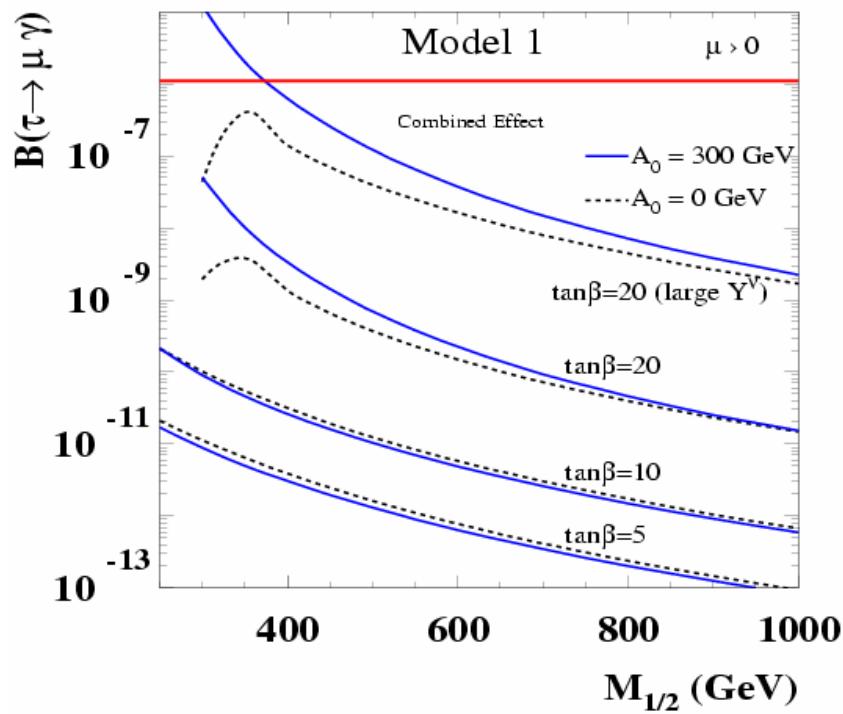
$$\delta A_{ij}^e \simeq -M_{\lambda_F} g_F^2 Y_{ij}^e Z_{ij}^e \frac{\ln (M_{st}/M_F)}{4\pi^2}$$

# $\mu \rightarrow e\gamma$ in Anomalous $U(1)$ Models



Enkhbat, Gogoladze, KSB (2003)

# $\tau \rightarrow \mu\gamma$ in Anomalous $U(1)$ Models



Enkhbat, Gogoladze, KSB (2003)

# Electric Dipole Moments of the leptons and the neutron

$$\mathcal{L}_{eff} = -\frac{i}{2} d_f \bar{\psi} \sigma_{\mu\nu} \gamma_5 \psi F^{\mu\nu}$$

**Violates CP**

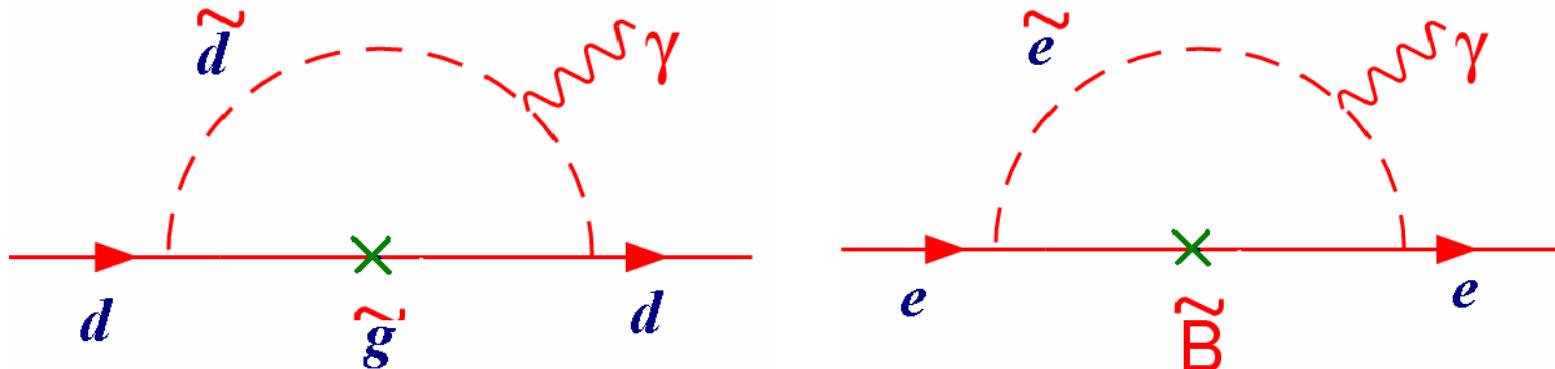
Electron:  $d_e(\text{Exp}) \leq 1.6 \times 10^{-27} \text{ e-cm}$

Muon:  $d_\mu(\text{Exp}) \leq 1.2 \times 10^{-18} \text{ e-cm}$

Neutron:  $d_n(\text{Exp}) \leq 6.3 \times 10^{-26} \text{ e-cm}$

**Phases in SUSY breaking sector contribute to EDM.**

## SUSY Contributions:



A, B are complex in MSSM

$$d_n \sim (\sin \phi) 10^{-23} \text{ e-cm}$$

$$d_e \sim (\sin \phi) 10^{-24} \text{ e-cm}$$

$$\Rightarrow \phi \simeq 10^{-2} - 10^{-1}$$

If SUSY-breaking parameters are all real, EDMs can still arise from neutrino Yukawa couplings

$$d_e \sim 10^{-31} \text{ e-cm}$$

Ellis et al (2002)

## EDM from Flavor Symmetry

The EDM induced by the  $U(1)_A$  flavor gaugino is estimated to be

$$d_e/e \simeq \frac{\alpha v_d M_{\tilde{B}}}{8\pi \cos^2 \theta_W} \frac{1}{m_{\tilde{l}}^2} A \left( \frac{M_{\tilde{B}}^2}{m_{\tilde{l}}^2} \right) \frac{(|q_s|g_F)^2 \log(M_{st}/M_F)}{8\pi^2} \sum_{i=2,3} \left[ C_i^m + C_i^A \right] \text{Im} \left[ \frac{Y_{1i}^e Y_{i1}^e}{Y_{ii}^e} \right],$$

$$C_i^m = \frac{(|q_s|g_F)^2 \log(M_{st}/M_F)}{8\pi^2} \frac{m_0^4 (A_0 - |\mu| \tan \beta)}{m_{\tilde{l}}^6} H_i^L H_i^R,$$

The flavor dependent factors:

$$H_i^L = 4 \left( M_{1/2}/m_0 \right)^2 \left( (q_i^L)^2 - (q_1^L)^2 \right) - (q_i^L - q_1^L) \text{Tr}(q) \text{ and } H^R = H^L (q^L \rightarrow q^e),$$

$$C_i^A = 2 \frac{M_{1/2}}{m_{\tilde{l}}^2} (Z_{i1}^e - Z_{11}^e).$$

$C^m$ —soft mass corrections,  $C^A$ — $A$ —term corrections

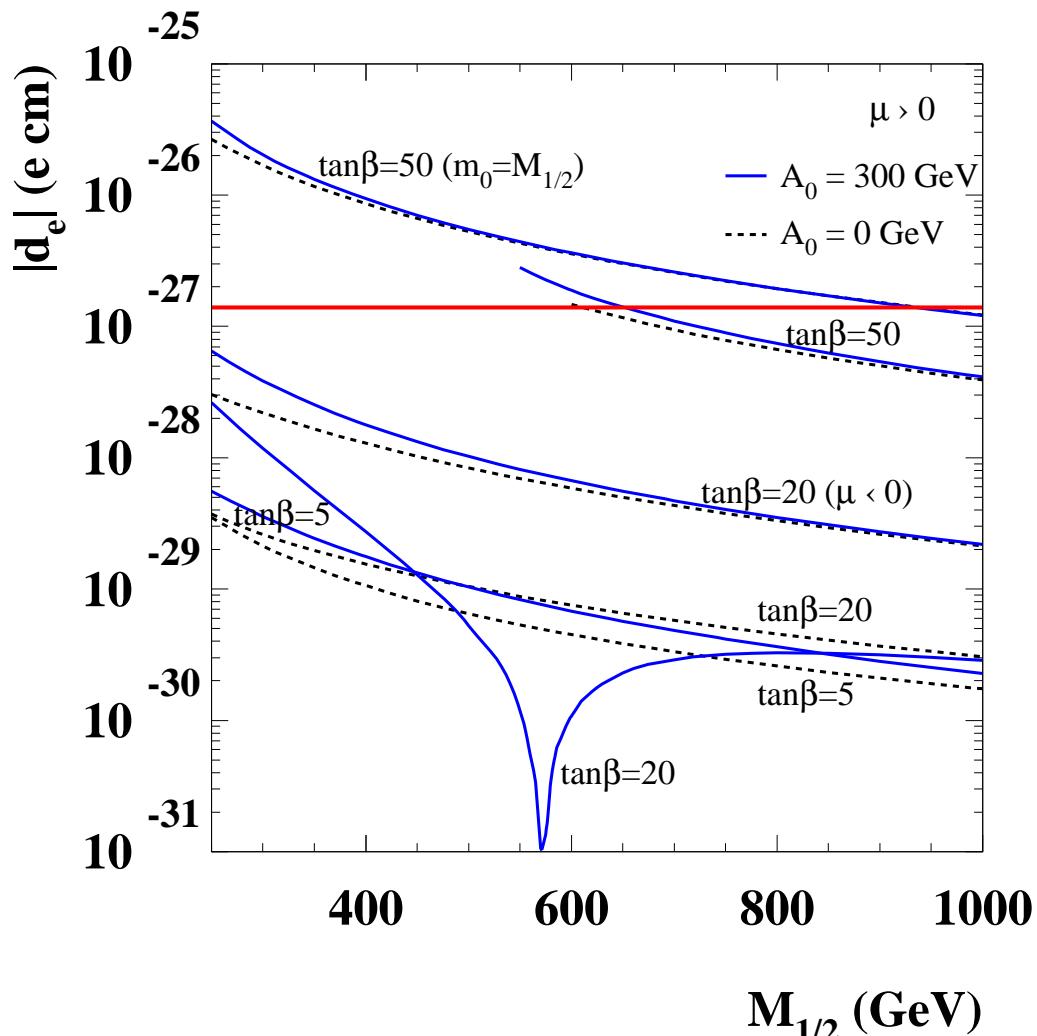


Figure 4: The Electron Electric Dipole Moment. The red line: experimental bound

Ts. Enkhbat, KSB, hep-ph/0406003

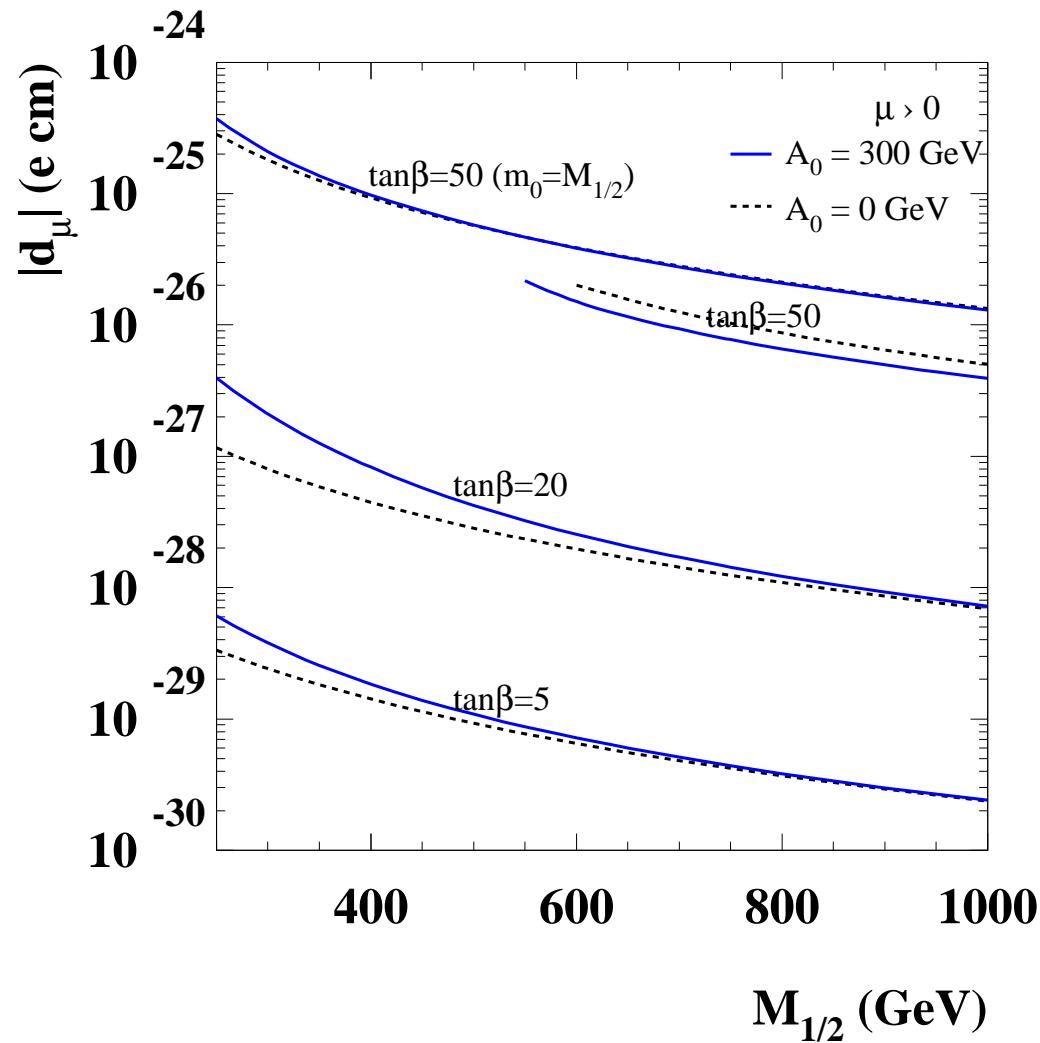


Figure 5: Muon Electric Dipole Moment.

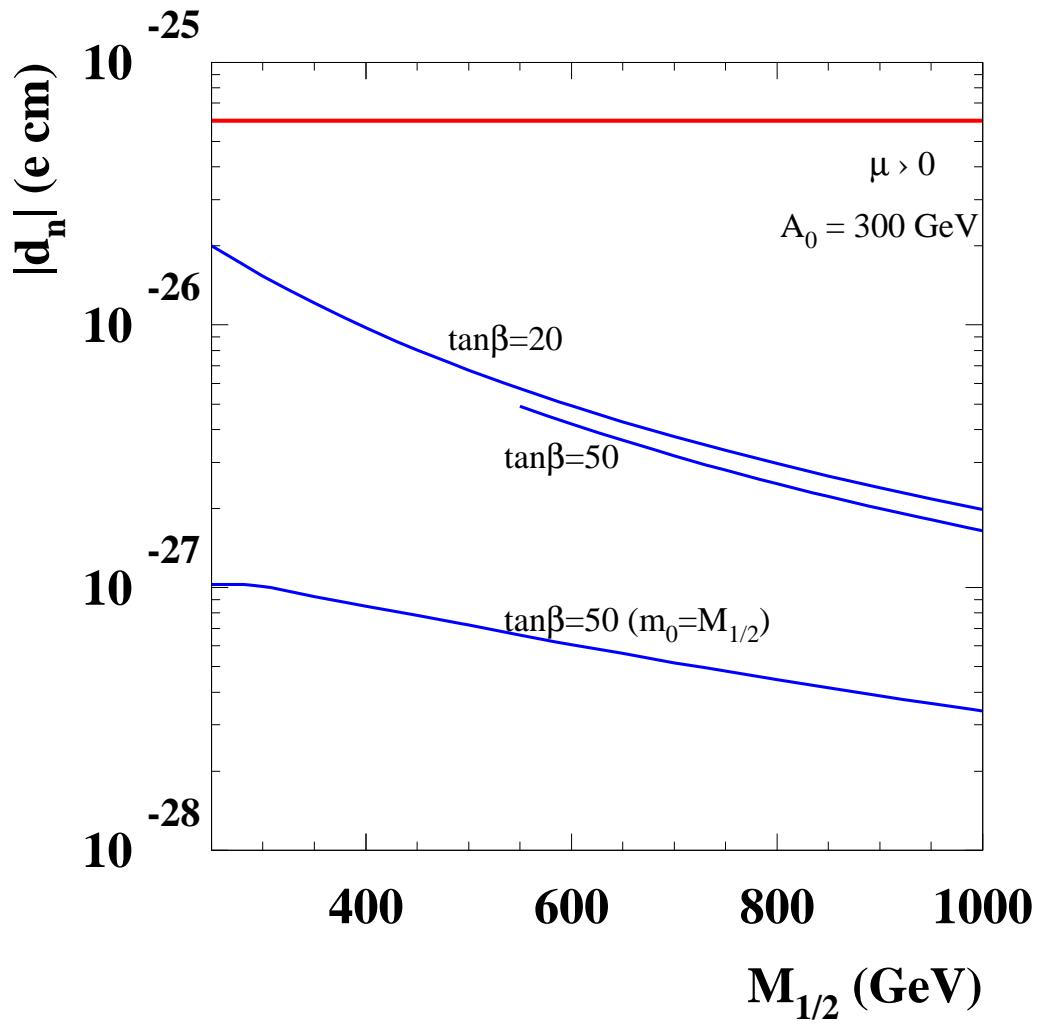


Figure 6: Neutron Electric Dipole Moment.

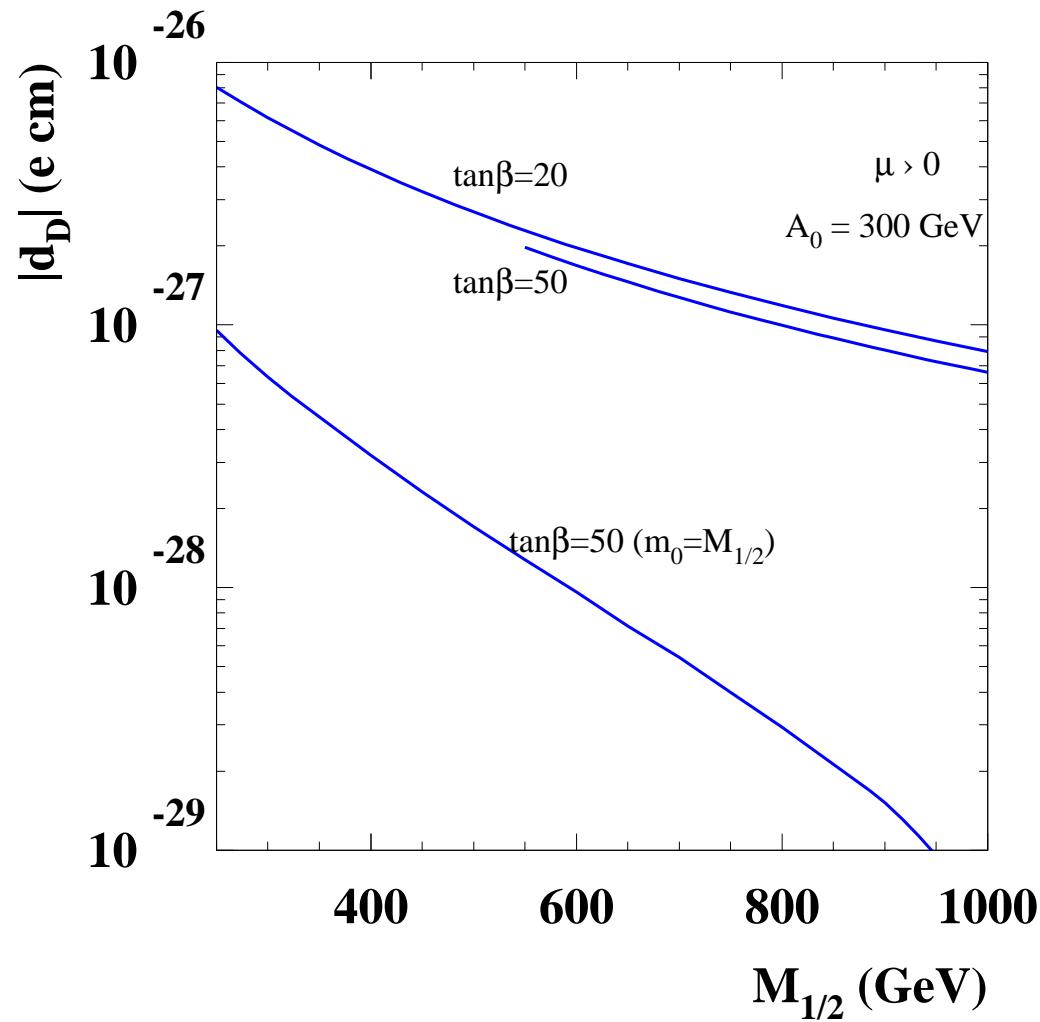


Figure 7: Deuteron Electric Dipole Moment.

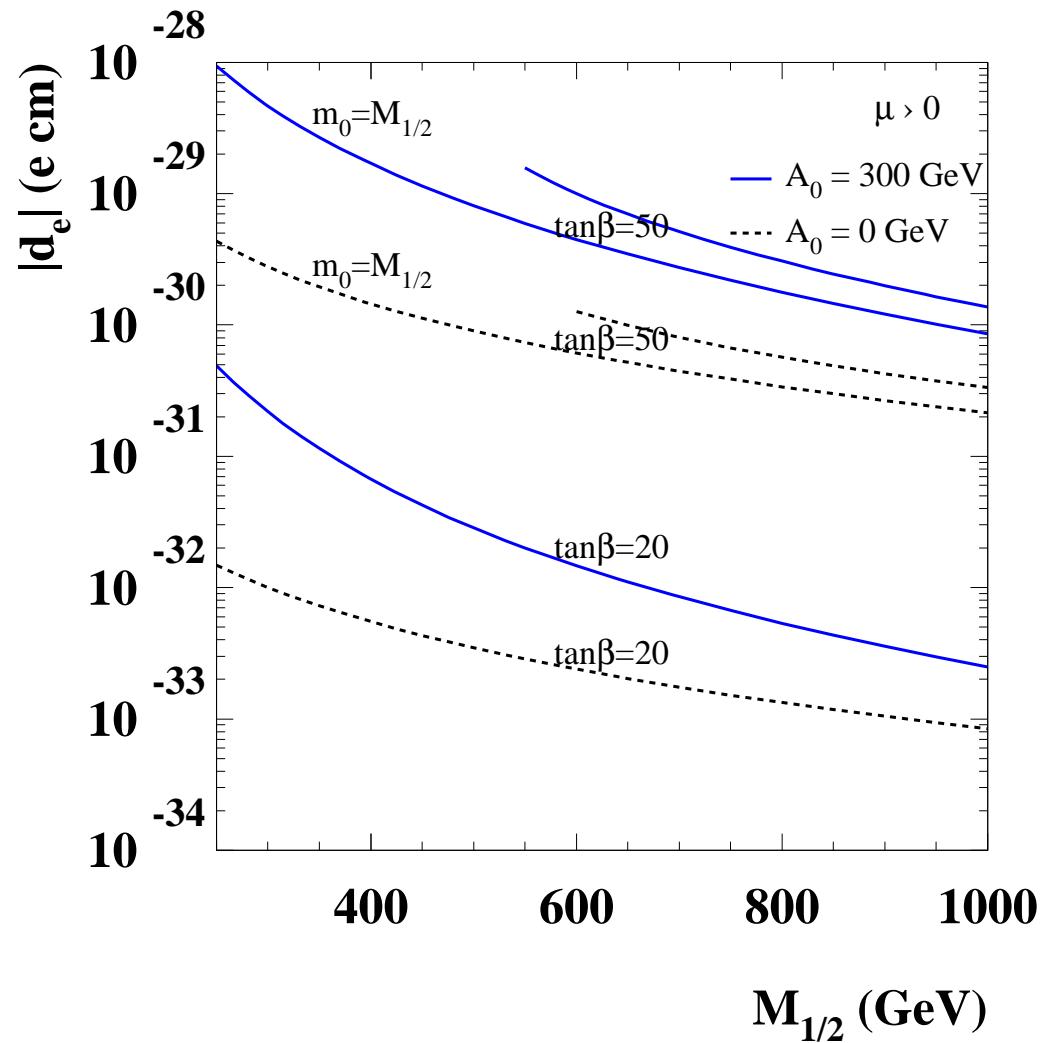


Figure 8: Electron Electric Dipole Moment by purely the neutrino effects.

**Parity Symmetry and EDM:** If parity is realized asymptotically,

$Y_U, Y_D, Y_E$       HERMITIAN

$A_U, A_D, A_E$       HERMITIAN

$f$       Complex Symmetric

EDM will arise only through non-hermiticity induced by RGE.

$$d_e \simeq 10^{-28} - 10^{-27} \text{ e-cm};$$

$$d_n \simeq 10^{-26} - 10^{-27} \text{ e-cm}$$

Subject to experimental tests

$$d_\mu = 10^{-22} - 10^{-23} \text{ e-cm}$$

Dutta, Mohapatra, KSB (2001)

## Scaling of Lepton EDM with Lepton Mass

Lepton Dipole Moment Matrix  $D$ :

$$D_{ij} \sim d_\tau \begin{pmatrix} (m_e/m_\tau)^3 + c \frac{\alpha}{4\pi} (m_e/m_\tau) & - & - \\ (m_e m_\mu^2/m_\tau^3) & (m_\mu/m_\tau)^3 & - \\ (m_e/m_\tau)^2 & (m_\mu m_\tau) & 1 \end{pmatrix}.$$

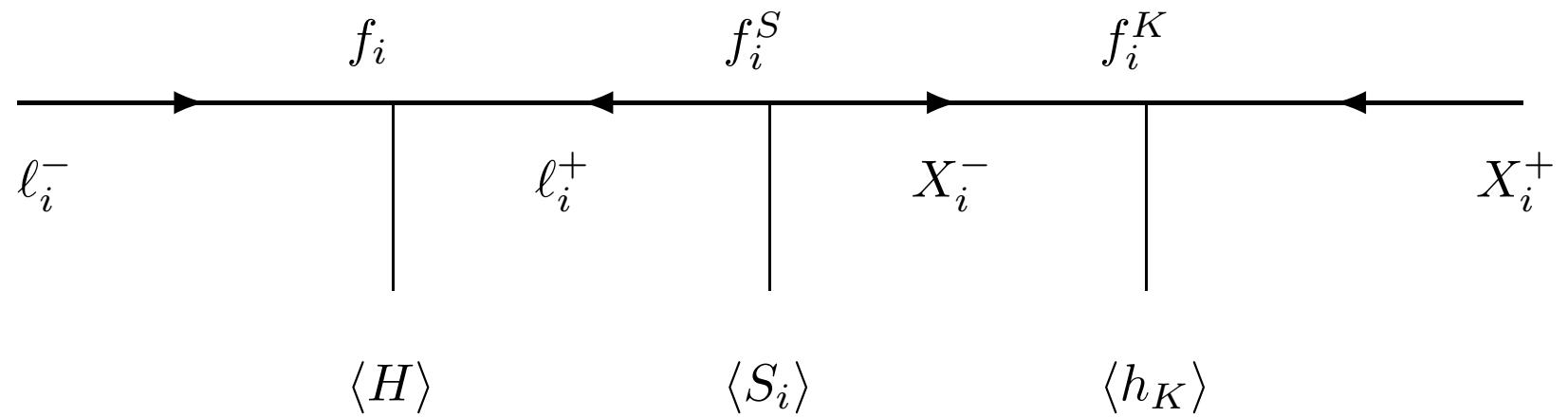
Here  $e, \mu, \tau$  obtain masses by mixing with exotic leptons  $X$ .

$$(\ell_{iL}^-, X_{iL}^-) \begin{pmatrix} \hat{m}_i & 0 \\ M_i & \langle F_i \rangle \end{pmatrix} \begin{pmatrix} \ell_{iL}^+ \\ X_{iL}^+ \end{pmatrix}.$$

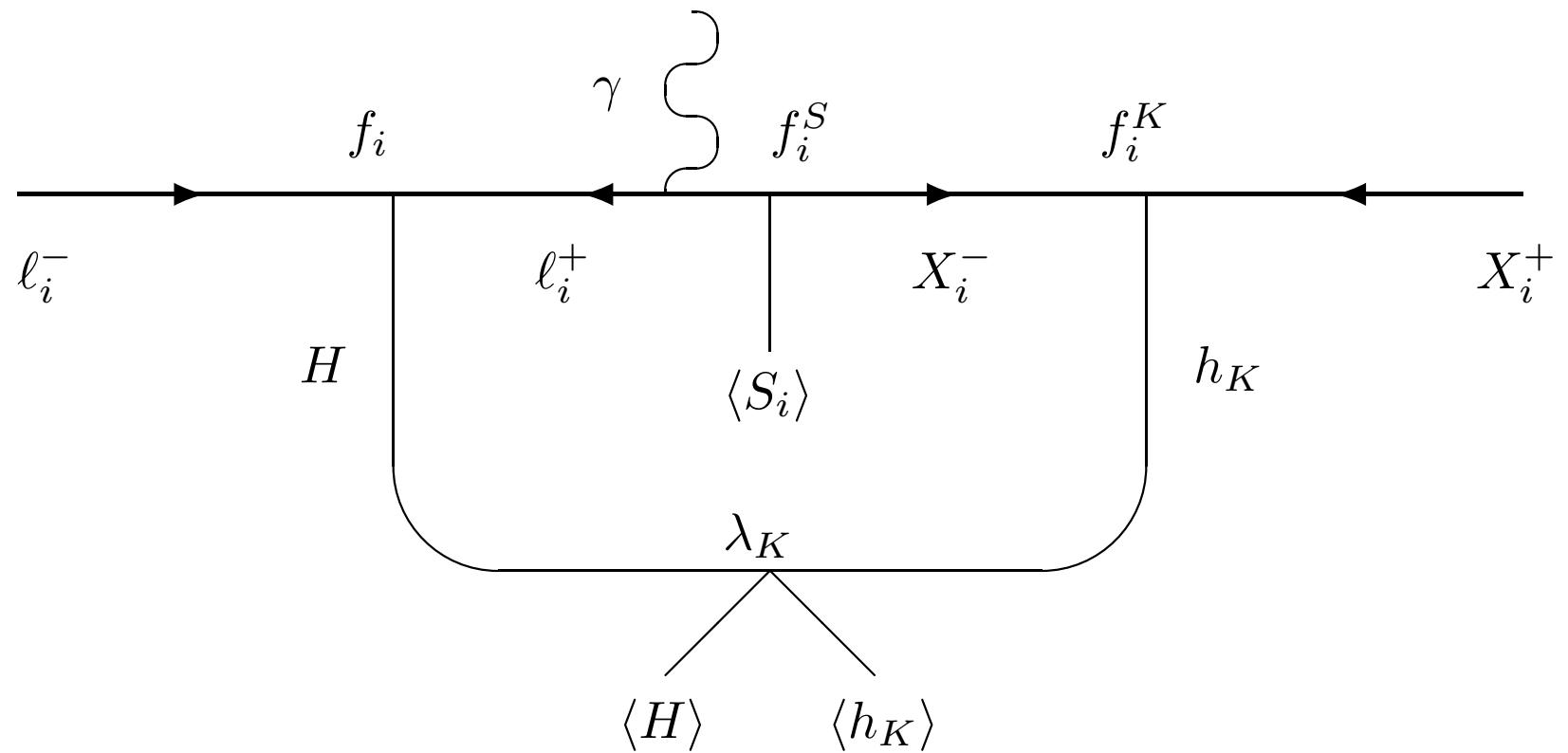
Lepton EDM given by

$$d_i \cong \frac{3e}{32\pi^2} \lambda_i \frac{\hat{m}_i \langle F_i \rangle}{M_i^3} = \frac{3e}{32\pi^2} \lambda_i \frac{m_i}{M_i^2}.$$

For  $M \sim 1 \text{ TeV}$ ,  $d_\mu \sim 3 \times 10^{-23} e \text{ cm.}$  S. Barr, KSB (2001)



**Fig. 2(a)**



**Fig. 2(b)**

# Conclusions

- Muons can serve as powerful probes of physics beyond the Standard Model
- Supersymmetry naturally leads to large corrections to muon g-2
- Supersymmetric seesaw mechanism suggests observable  $\mu \rightarrow e\gamma$  rate
- Flavor symmetry for fermion masses and mixings leads to sizable  $\mu \rightarrow e\gamma$  rate and EDM
- Leptonic EDM need not scale linearly with lepton mass
- Large neutrino mixing may indicate muon EDM as large as  $10^{-22}$  e cm